Vacuum-enhanced optical nonlinearities with disordered molecular photoswitches

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It is well known that nonlinear optical signals such as cross-phase modulation can be coherently enhanced in multilevel atomic gases under conditions of electromagnetically induced transparency, but analogous results in solids are challenging to obtain due to natural energetic disorder. We propose a solid-state cavity QED scheme to enable cross-phase modulation between two arbitrarily weak classical fields in the optical domain, using a highly disordered intracavity medium composed of organic molecular photoswitches. Even in the presence of strong energetic and orientational disorder, the unique spectral properties of organic photoswitches can be used to enhance the desired nonlinearity under conditions of vacuum-induced transparency, enabling cross-phase modulation signals that surpass the detection limit imposed by absorption losses. Possible applications of the scheme include integrated all-optical switching with low photon numbers.

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The generation of nonlinear optical signals in solids requires the use of intense lasers because the nonlinear susceptibility of materials is small and difficult to manipulate. On the other hand, the optical response of atomic gases can be routinely manipulated via quantum interference effects such as coherent population trapping (CPT) [1] and electromagnetically induced transparency (EIT) [2], which has enabled the development of quantum memories [3] based on slow light [4], atomic clocks [5], and nonlinear optics at the level of individual photons [6]. In solids, coherent optical schemes analogous to those observed in atomic gases have been implemented with rare-earth doped crystals [7], quantum wells [8], and quantum dots [9] in samples with negligible inhomogeneous broadening at cryogenic temperatures. Attempts to implement coherent optical schemes with inhomogeneously broadened NV centers in diamond [10,11] have shown that unavoidable static energy fluctuations in the system severely restrict the quality of the quantum interference effects responsible for EIT. In atomic gases, it is always possible to suppress the detrimental effects of inhomogeneous broadening due to the Doppler shift of the transition frequencies involved, by adjusting the propagation direction, frequency, and intensity of the driving lasers [12]. However, no analogous mechanism is known for compensating static energy level fluctuations in the condensed phase.

In recent years, the demonstration of the strong and ultrastong coupling regimes of cavity quantum electrodynamics (QED) at room temperature with organic molecular emitters in optical microcavities [13–17] has stimulated the development of integrated quantum technology that exploits quantum optics to enhance the natural transport and optical properties of organic materials [18–22]. However, efforts for exploiting strong coupling in microcavities to establish CPT and EIT with molecular aggregates have failed because energy disorder unavoidably degrades the electronic interference necessary to establish coherent optical effects [23], even at cryogenic temperatures.

We develop a theory for a solid-state cavity QED scheme to implement vacuum-induced transparency (VIT) [24,25] as well as cross-phase modulation (XPM) between two arbitrarily weak coherent fields that interact with a strongly disordered medium composed of organic molecular photoswitches [26–28]. Achieving VIT is a prerequisite for coherence-based XPM with low photon numbers [29]. In this Rapid Communication, we extend the theory in Ref. [29], which is valid only for homogeneously broadened atomic gases, by taking into account the dominant role of inhomogeneous broadening due to static electronic energy disorder on all the molecular transitions involved. Our analysis is motivated by unique features in the electronic structure of organic photoswitches that are not present in other molecular species. We show that organic photoswitches can naturally support conditions for VIT in high-quality nanoscale optical cavities, despite strong energy disorder.

The envisioned light-matter scheme is shown in Fig. 1. The ground electronic potential of the photoswitch (S0) has two deep wells in the isomerization coordinate corresponding to the cis and trans molecular isomers [26]. The lowest vibrational state of the trans isomer is the stable ground state of the system [1]. The metastable ground state [2] corresponds to the lowest vibrational level of the cis isomer potential well. Thermal isomerization of state [2] is energetically forbidden at room temperature [26]. The lowest excited potentials S1 and S2 [30] correspond to states [3] and [4], respectively. The vibrational structure of the excited potentials is not resolved in condensed phase, but S0 has spectrally resolved torsional modes with frequencies in the range \( \omega_\text{c} \sim 160–190 \text{ meV/}h \) [31].
Our model does not require an exact knowledge of the molecular potentials. Instead, we impose a set of constraints on the inhomogeneously broadened photoswitch absorption spectrum outside the cavity, which we illustrate in Fig. 1(b). The photoswitch spectrum should have (i) a well-resolved band associated with the cis transition $|2\rangle \rightarrow |3\rangle$, resonant with the cavity frequency $\omega_c$, (ii) a well-resolved band associated with the trans transition $|1\rangle \rightarrow |3\rangle$, near resonant with the probe frequency $\omega_p > \omega_c$, and (iii) a well-resolved band associated with the cis transition $|2\rangle \rightarrow |4\rangle$, weakly driven by a blue-detuned signal field at frequency $\omega_s > \omega_p$. These spectral requirements can be met by orthogonal molecular photoswitches [32–34].

For a single emitter, the light-matter coupling scheme in Fig. 1 can be modeled by the Hamiltonian

$$
\hat{H}_S = \omega_c \hat{a}^\dagger \hat{a} + \omega_{21} \hat{a}^\dagger |2\rangle \langle 2| + \omega_{31} |3\rangle \langle 3| + \omega_{31} |4\rangle \langle 4| + \Omega_p (|3\rangle \langle 2| + |2\rangle \langle 3|) e^{i\omega_p t}/\Gamma_1 + |1\rangle \langle 3| e^{i\omega_q t} + \Omega_p (|4\rangle \langle 2| - |2\rangle \langle 4|) e^{i\omega_p t}/\Gamma_1,$n

(1)

where $\Omega_p$ and $\Omega_q$ are the probe and signal semiclassical Rabi frequencies, respectively. $\Omega_c$ is the cavity vacuum Rabi frequency, and $\hat{a}$ is the annihilation operator of the cavity field. In a dressed-state picture, our electronic basis must be supplemented with the cavity states to read $|\tilde{1}\rangle \equiv |1;0_c\rangle$, $|\tilde{2}\rangle \equiv |2;1_c\rangle$, $|\tilde{3}\rangle \equiv |3;0_c\rangle$, and $|\tilde{4}\rangle \equiv |4;1_c\rangle$. The probe field thus drives the transition $|\tilde{1}\rangle \leftrightarrow |\tilde{3}\rangle$, the signal field the transition $|\tilde{2}\rangle \leftrightarrow |\tilde{4}\rangle$, and the cavity field strongly admixes the nearly degenerate dressed states $|\tilde{2}\rangle$ and $|\tilde{3}\rangle$.

We model energy disorder in the Hamiltonian $\hat{H}_S$ by defining the random transition frequencies $\omega_{31} = \langle \omega_{31} \rangle + \delta_{31}$, $\omega_{32} = \langle \omega_{32} \rangle + \delta_{32}$, and $\omega_{32} = \langle \omega_{32} \rangle + \delta_{32}$, where $\langle \omega_{ij} \rangle$ corresponds to the band center frequency and $\delta_{ij}$ is a random static fluctuation that gives rise to the inhomogeneous linewidths $\sigma_{ij}$. Linewidths due to energy disorder are typically in the range 150–200 meV for organic photoswitches [35], magnitudes that far exceed the typical homogeneous linewidth. In addition to energy disorder, below we also model orientational disorder in the system by writing the vacuum Rabi frequency as $\Omega_c = \Omega_c \cos \theta$, where $\Omega_c$ is a constant amplitude and $\theta$ is a uniformly distributed random angle between the molecular transition dipole moment and the space-fixed cavity field polarization.

In general, the ultrafast dynamics of photoisomerization involves a complex interplay between nonadiabatic coupling and nonsecular relaxation [36]. Since we are only interested in the steady-state response of the cavity subject to continuous driving, we ignore the transient femtosecond dynamics of the system and adopt a coarse-grained Lindblad quantum master equation to describe dissipation. The bare photon lifetime is assumed in the range 1/$\kappa \sim 10–100$ ps, which can be achieved using high-$Q$ dielectric cavities [37]. Nonradiative decay of the excited state $S_2 \rightarrow S_1$ by intramolecular vibrational relaxation (IVR) has a lifetime 1/$\Gamma_{\text{IVR}} \sim 0.1$ ps [38]. Nonradiative decay $S_1 \rightarrow S_0$ into the trans and cis ground states occurs at the rates $\Gamma_{31}$ and $\Gamma_{32}$, respectively. The homogeneous probe absorption linewidth is defined as $\gamma = \Gamma_{31} + \Gamma_{32}$, with typical excited-state lifetimes in the range 1/$\gamma \sim 0.1–0.5$ ps [35,39]. Finally, we account for pure dephasing of the coherence between the vibrational ground states $|1\rangle$ and $|2\rangle$ at the rate $\Gamma_{pd}$, with typical dephasing times in the range 1/$\Gamma_{pd} \sim 1–100$ ps [40–43], depending on the molecular species, solvent, and temperature.

We derive an expression for the disorder-free susceptibility of the organic medium at the probe frequency $\chi_p$, as described in Sec. S1 of the Supplemental Material (SM) [44]. We then obtain the disorder-averaged susceptibility $\langle \chi_p \rangle$ by analytically integrating over random dipole orientations $\theta$ and over the random frequency shifts $\delta_{ij}$. The results are used to describe the photophysics of inhomogeneously broadened molecular photoswitches in nanoscale optical cavities.

We begin by assuming that no signal field is present ($\Omega_q = 0$). In Fig. 2, we show the corresponding disorder-averaged susceptibility $\langle \chi_p \rangle$ as a function of the mean probe detuning $\Delta_p = \omega_p - \langle \omega_{31} \rangle$, for the representative decay ratios...
the vibrational ground states to fluctuate independently, where \( \delta \) is the detuning. The survival of VIT in the presence of disorder [21] would require that \( \delta_1 = \delta_2 \) (green). Solid and dashed lines correspond to signal-to-noise ratios below unity. We use \( \gamma_s = 2 \times 10^{-5} \gamma \) and \( \Omega_s = 0.8 \gamma \) in both panels.

\[ \Gamma_{pd}/\gamma = 10^{-2} \text{ and } \kappa/\gamma = 10^{-4}. \] We numerically average the homogeneous response over a large number of disorder configurations. For the orientational average, Figs. 2(a) and 2(b) confirm that random dipole orientations do not significantly alter the coherent optical properties of cavity states [45]. The analytical average in Eq. (S16) of the SM coincides exactly with the numerical average.

We numerically average energy disorder by taking random frequency fluctuations \( \delta_{ij} \) from independent Gaussian distributions with the same standard deviation, i.e., \( \sigma_{ij} = \sigma \). Figures 2(c) and 2(d) show the characteristic signatures of VIT despite inhomogeneous broadening due to energy disorder (\( \sigma = 6\gamma \)): strong suppression of the probe absorption (transparency) and steep dispersion (slow light), over a narrow frequency window around the two-photon resonance condition \( \Delta_p - \Delta_s = 0 \) [2], with \( \Delta_s \equiv \omega_s - (\omega_{s2}) \) being the cavity detuning. The survival of VIT in the presence of disorder can be understood analytically by averaging \( \langle \chi_p \rangle \) using a Lorentzian disorder model, as discussed in Sec. S2-B of the SM. The Lorentzian model is found to underestimate the quality of VIT in comparison with a more realistic Gaussian disorder, as Fig. 3(b) below shows. Within the Lorentzian model, the homogeneous linewidth \( \gamma_s \) associated with transition \( |i \rangle \leftrightarrow |j \rangle \) is simply replaced by \( \Sigma_{ij} = \gamma_{ij} + \sigma_{ij} \), i.e., the inhomogeneous linewidth is just an additive contribution to the total linewidth. This result also holds for XPM, as discussed below. For a disorder-free system (e.g., atomic gases), a high-visibility VIT signal would require that \( \gamma_{21} \ll \Omega_s \ll \gamma \) [24]. As long as disorder only affects the probe transition \( |1 \rangle \rightarrow |3 \rangle \), we can rewrite these conditions as follows,

\[ \gamma_{21} \ll \Omega_s \ll \Sigma_{31}, \] where \( \gamma_{21} \equiv \kappa/2 + \Gamma_{pd} \) is the decay rate of the coherence between dressed states \( |1 \rangle \) and \( |2 \rangle \), and \( \Sigma_{31} \equiv (\gamma/2 + \sigma_{31}) \) is the total probe \textit{trans} absorption linewidth, with \( \sigma_{31} \) being the inhomogeneous contribution. This result requires that the static energy fluctuations of states \( |1 \rangle \) and \( |2 \rangle \) are equal, i.e., \( \delta_{31} = \delta_{32} \). The quality of VIT degrades as we allow the two ground isomer potential minima to fluctuate independently, setting a constraint on the contribution of inhomogeneous broadening on the vibrational Raman frequency \( \omega_{s2} \) to be much smaller than the excited-state linewidth \( \gamma \). If \( \omega_{s2} \) were to fluctuate significantly, the inaccuracy Raman dark state \(|D\rangle = \sqrt{\sigma} |1 \rangle + \sqrt{1-\sigma} |2 \rangle \) \((0 < \sigma < 1) [2] \) would rapidly dephase, breaking the CPT effect that causes the VIT.

In molecular photoswitches, both \textit{cis} and \textit{trans} isomers belong to the same molecular orbital. Therefore, we expect that \( \delta_{31} = \delta_{32}/\gamma \gg 1 \) in a condensed-phase environment, enabling conditions for VIT. This would not be the case if the vibrational ground states \(|1 \rangle \) and \( |2 \rangle \) belong to different molecular orbitals, highlighting the unique features of organic photoswitches over other molecular species for the implementation of coherent optics in condensed phase.

Having established the physical conditions for achieving VIT with disordered molecular photoswitches, we now discuss the desired XPM scheme involving simultaneous driving of the intracavity medium with both probe and signal fields. We focus on the phase shift \( \Phi \) experienced by the probe field due to copropagation with a signal field over a given path length. Attenuation at the probe frequency is quantified by the absorption coefficient \( \alpha \). Under conditions of VIT, both \( \Phi \) and \( \alpha \) not only depend on the probe and signal field frequencies and Rabi frequencies, but also on the cavity vacuum parameters [24,46]. Following Ref. [47], we define the figure of merit \( \langle \eta_p \rangle = \text{Re}(\chi_p)/2 \text{Im}(\chi_p) \) to quantify the degree by which it is possible to interferometrically resolve the XPM phase shift \( \Phi \) at frequency \( \omega_p \). Detectable nonlinear signals require \( \langle \eta_p \rangle > 1 \).

In Sec. S3 of SM, we develop an analytical approximation for the disorder-averaged susceptibility \( \langle \chi_p \rangle \) in the presence of both probe and signal fields. We integrate the disorder-free susceptibility over the random fluctuations \( \delta_{31}, \delta_{32} \) assuming that they belong to independent Lorentzian distributions with different widths. Lorentzian averaging compares well with Gaussian disorder for \( \Omega_s = 0 \) [12,48], and is analytically tractable for the analysis of cross-phase modulation signals. We derive an expression for \( \langle \chi_p \rangle \) in Eq. (S19) in SM, from which we can write the mean figure of merit

\[ \langle \eta_p \rangle = \frac{1}{2} \frac{\Omega_s^2 (x - x_s) - x A_s(x)}{\Sigma_{31} A_s(x) + \Omega_s^2 (\gamma_{21} + \gamma_s)} \] (3)

where \( x \equiv \Delta_p \) is the probe detuning. The function \( A_s(x) \equiv (x - x_s)^2 + (\gamma_{21} + \gamma_s)^2 \) is given in terms of the frequency shift \( x_s \equiv \lambda_s \Delta_s \) and width \( \gamma_s \equiv \lambda_s \Sigma_{41} \), with all the signal properties are combined into the parameter

\[ \lambda_s \equiv \Omega_s^2 / (\Delta_s^2 + \Sigma_{41}^2) \] (4)

where \( \Delta_s = \omega_s - (\sigma_{42}) \) is the mean signal detuning and \( \Sigma_4 \equiv \kappa/2 + \Gamma_{VR}/2 + \sigma_{42} \), where \( \sigma_{42} \) is the inhomogeneous linewidth of the \textit{cis} absorption band. In Sec. S4-B of the SM, we show that \( \lambda_s \) exclusively captures the effect of the signal field on \( \langle \chi_p \rangle \).

Outside the cavity (\( \Omega_s = 0 \)), Eq. (3) simply reduces to the linear response result \( \langle \eta_p \rangle = -\Delta_p/2\Sigma_{31} \), which near resonance gives \( \langle \eta_p \rangle \ll 1 \) due to absorption of the probe field. In the presence of the cavity vacuum, but without signal driving (\( \Omega_s = 0 \)), the figure of merit \( \langle \eta_p(\Omega_s = 0) \rangle \equiv \langle \eta_{\text{VIT}} \rangle \) can be considered as a degree of coherence in the response of the
medium to the probe field. In this VIT regime, Eq. (3) reduces to Eq. (S21) of the SM, which can be written as
\[
\langle \eta_{\text{VIT}}(x) \rangle \approx \frac{\Omega_{x}^{2}}{2(\Sigma_{31} x^{2} + \gamma_{21} \Omega_{x}^{2})} \gg 1, \tag{5}
\]
when \( \gamma_{21} \ll x \ll \Omega_{x} \).

For a system dominated by inhomogeneous broadening (\( \gamma \ll \Omega_{31} \)) and a long-lived dressed vibrational coherence (\( \gamma_{21} \ll \gamma \)), Eq. (5) has a maximum at the probe detuning \( x_{s} = \Omega_{x} \sqrt{\gamma_{21}/\Omega_{31}} \) that is blueshifted from the VIT absorption minimum, giving the optimal figure of merit
\[
\langle \eta_{\text{VIT}}^{\text{max}} \rangle = \frac{\gamma_{s}}{\sqrt{16 \gamma_{21} \Omega_{31}}}. \tag{6}
\]

We next discuss the behavior of Eq. (3) under simultaneous probe and signal driving (\( \Omega_{s} > 0 \)), when the figure of merit is directly related to the magnitude of the XPM signal [47]. Coupling to the signal field tends to destroy VIT, by weakly admixing the dark state \( |D) \) (see above) with the fast-decaying excited dressed state \( |4⟩ \). The maximum achievable figure of merit \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \) subject to signal driving therefore cannot exceed the VIT maximum in Eq. (6), i.e., \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \leq \langle \eta_{\text{VIT}}^{\text{max}} \rangle \) for any \( \lambda_{s} \), with the equality sign holding only when \( \lambda_{s} = 0 \).

We can use Eq. (3) to find the constraints on \( x_{s} \) and \( \gamma_{s} \) that allow the nonlinear figure of merit to approach the VIT limit \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \). For instance, in realistic organic systems dominated by inhomogeneous broadening with \( \Sigma_{41} \approx \Sigma_{31} \approx \sigma \) and assuming \( \Omega_{x}/\Delta_{1} \approx \sqrt{\gamma_{21}/\sigma} \), our Lorentzian disorder model predicts that it is possible to reach \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \gg 1 \) under a single constraint on the dimensionless signal parameter, given by \( \lambda_{s} \approx \gamma_{21}/\sigma \ll 1 \). In summary, large values of \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \) can be reached by the following: (i) decreasing \( \Omega_{x} \), as the signal field partly destroys VIT, as it is not protected by the transparency window; (ii) increasing \( \Delta_{1} \), making the incoherent signal field less resonant and therefore less absorptive; and (iii) increasing \( \sigma_{41} \), effectively distributing the signal beam among many frequencies, many of which are far-detuned from \( \omega_{42} \) and therefore less absorptive.

We finally compare the predictions of our Lorentzian disorder model [Eq. (3)] with a Gaussian model, which is more experimentally relevant. Figure 3(a) shows the \( \eta(x) \) profiles predicted by the Lorentzian model and the result of numerical integration with \( b_{31} \) and \( b_{42} \) taken from independent Gaussian distributions, again assuming \( \delta_{31} = \delta_{42} \) as in Fig. 2.

We find that even when the Gaussian and Lorentzian noise distributions have equal widths [full width at half maximum (FWHM)], Gaussian disorder consistently allows for higher values of \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \). This behavior is captured in Fig. 3(b), which shows that for fixed \( \gamma_{21} \) and \( \sigma_{0} \), the XPM signal in systems with Gaussian absorption are detectable for values of \( \lambda_{s} \) that are nearly an order of magnitude higher than those predicted by the Lorentzian model, reducing the experimental constraints on the signal field. Figure 3(b) also shows that the Lorentzian model underestimates the asymptotic VIT bound on \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \) as \( \lambda_{s} \rightarrow 0 \).

By studying the dependence of the desired XPM signal on the dephasing rate \( \gamma_{21} \), we find that the scaling of the upper bound \( \langle \eta_{\text{VIT}}^{\text{max}} \rangle \sim \Omega_{x}/\sqrt{\gamma_{21}} \) predicted by the Lorentzian model [Eq. (6)] can also accurately describe the behavior of the upper bound for Gaussian disorder (see Fig. S3 of SM). In other words, a larger vacuum Rabi frequency \( \Omega_{x} \) can compensate for a large dephasing rate \( \gamma_{21} \), in order to achieve detectable XPM signals.

In summary, we propose an organic cavity QED scheme to achieve large cross-phase modulation signals using arbitrarily weak probe and signal fields, despite strong energetic and orientational disorder in the material. The scheme exploits a long-lived vibrational coherence between the cis and trans ground vibrational states in a class of chromophores known as molecular photoswitches, to establish conditions for VIT. In addition to conventional high-\( Q \) microcavities, the proposed scheme could be implemented with an ensemble of \( N \) nanoscale optical cavities, each containing a single molecular photoswitch with random dipole orientation and electronic energy gaps, within the cavity mode volume. Ensembles of single-emitter nanoscale organic cavities can been prepared and optically probed using nanophotonic techniques [49–51]. Our results thus pave the way for the development of organic-based integrated nanophotonic devices for all-optical switching at ultralow power levels.

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